

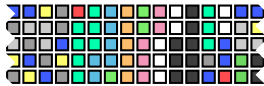
# Scalable Online First-Order Monitoring

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Srđan Krstić   Dmitriy Traytel

Department of Computer Science

**ETH** zürich

# Online Monitoring



event stream



monitor



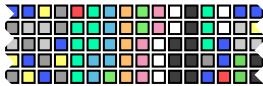
$\square \forall u. \forall dt.$

$\text{insert}(u, \text{db1}, dt) \wedge dt \neq \text{unknown} \rightarrow$

$\blacklozenge_{[0,1s]} \blacklozenge_{[0,30h]} \exists u'. \text{insert}(u', \text{db2}, dt) \vee \text{delete}(u', \text{db1}, dt)$

formal specification

# Online Monitoring



event stream

in-order  
unbounded



monitor



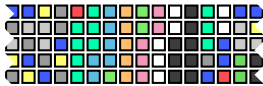
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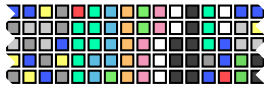


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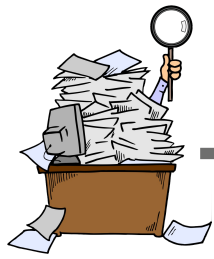
metric first-order temporal logic (MFOTL)

# Online Monitoring



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verdict stream

evaluated at every  
time-point

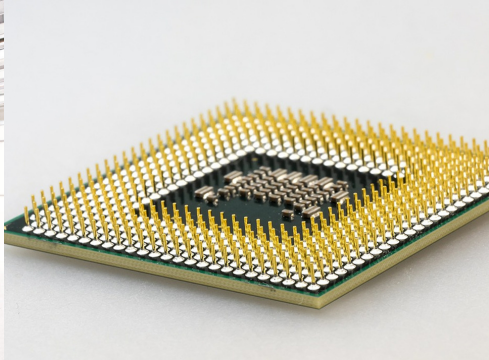
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**Scalable** online monitoring in the face of  
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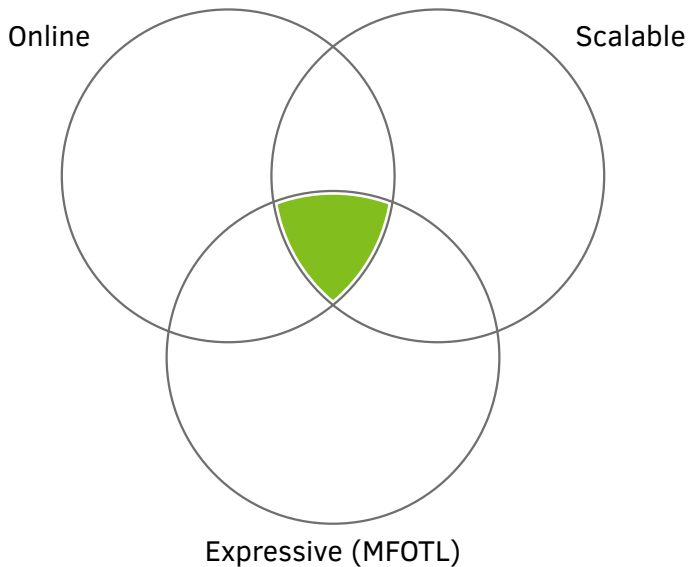
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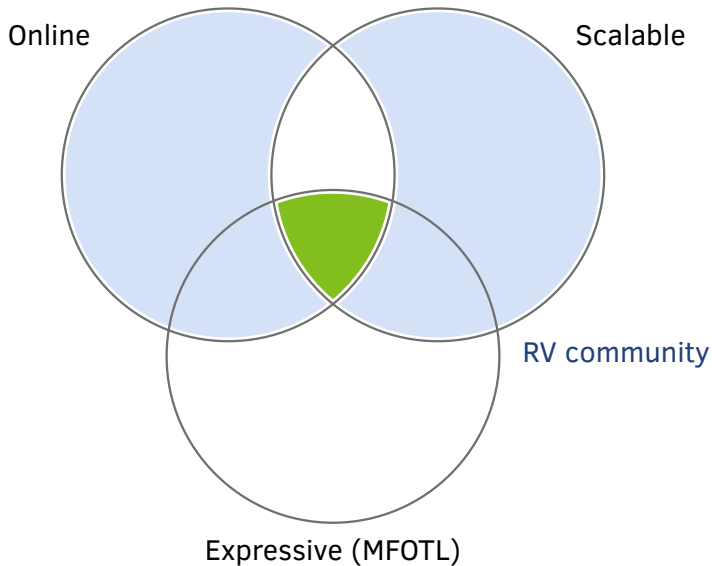
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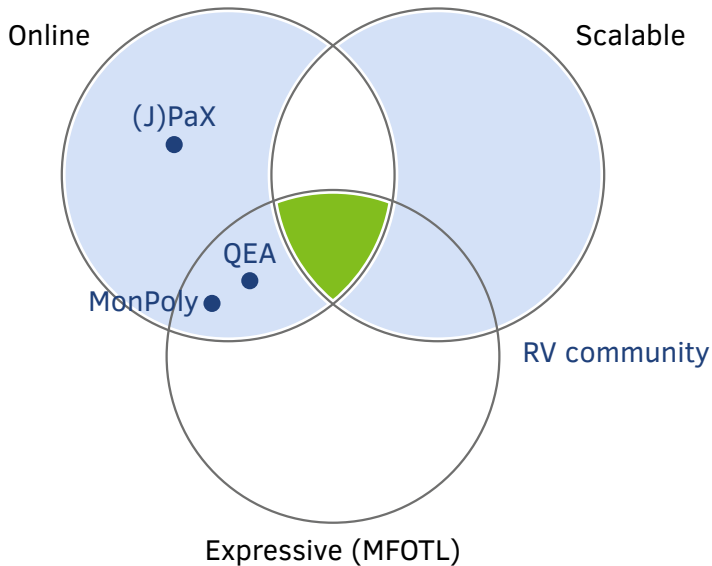
# Related Work



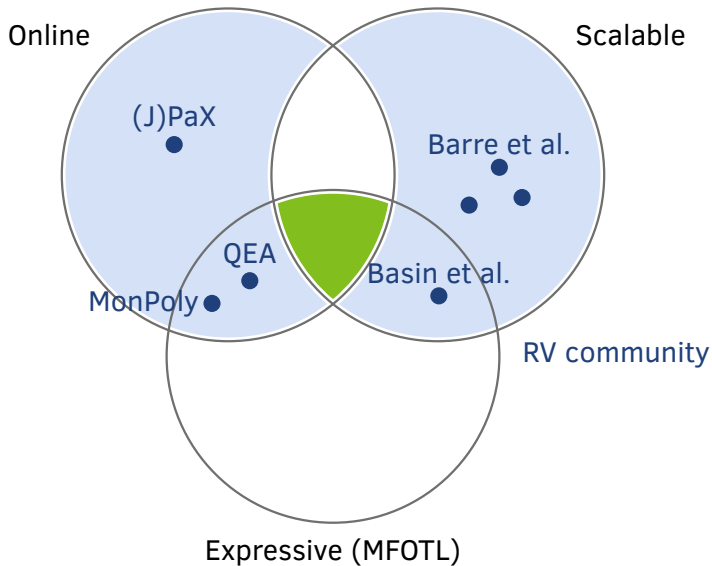
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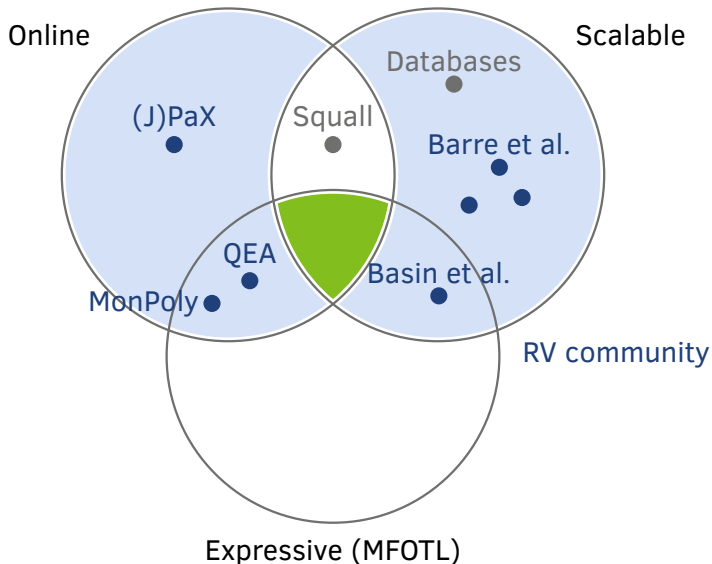
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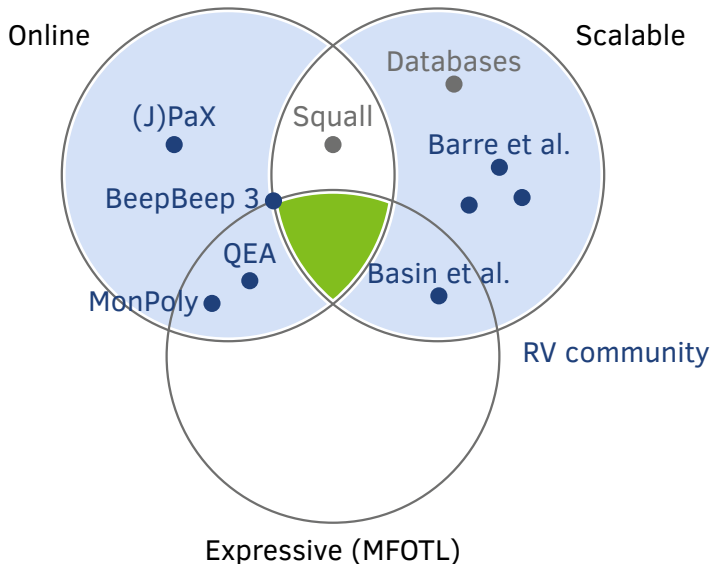
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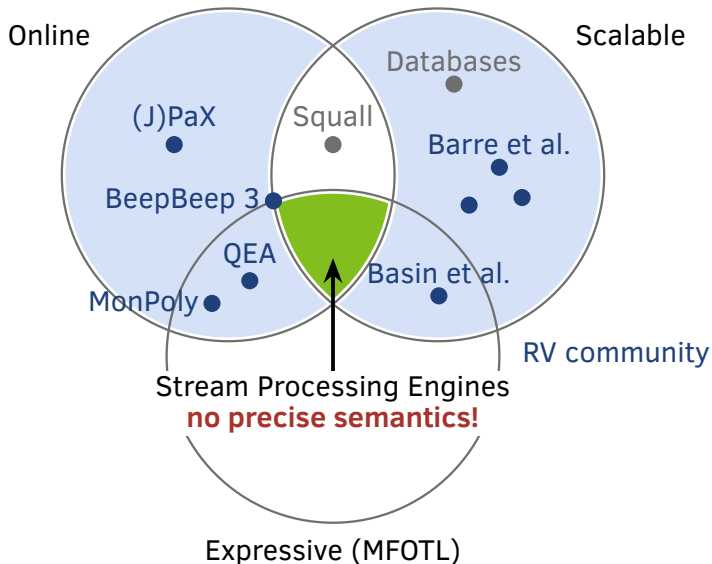


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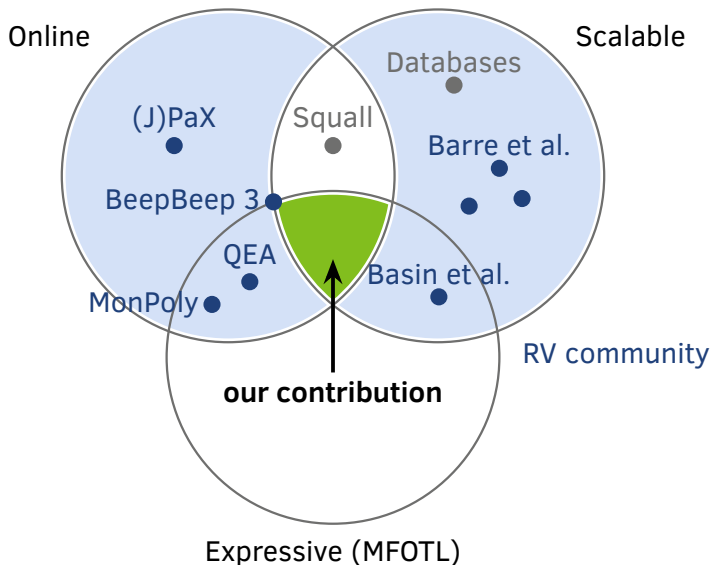




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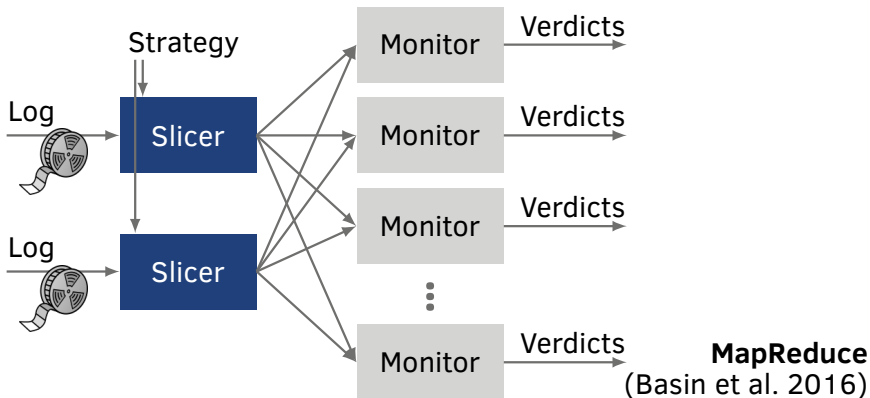
# Slicing the Event Stream

- **Reuse** existing monitoring algorithm (MonPoly)



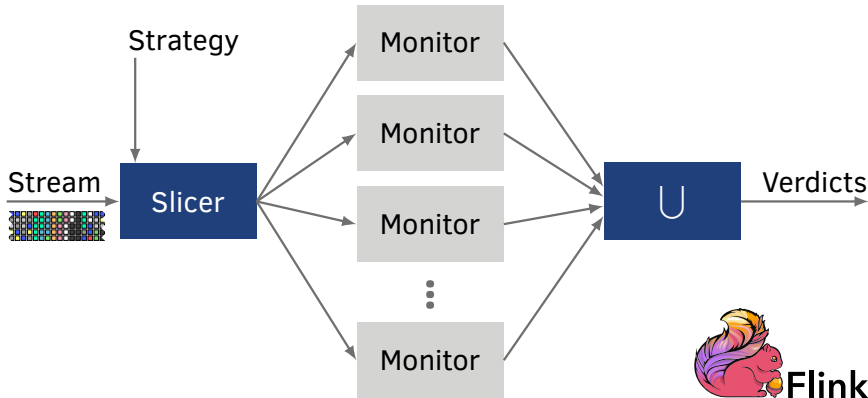
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- **Reuse** existing monitoring algorithm (MonPoly)
- **Split** event stream into slices



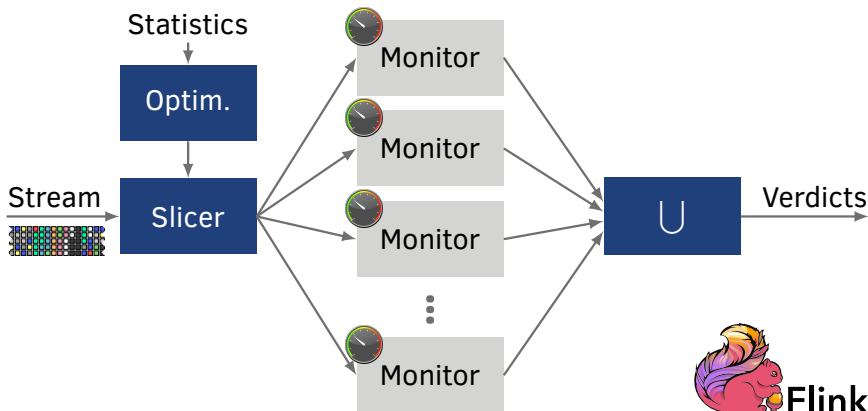
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# Prior Work: Offline Slicing

(Basin et al. 2016)

## Example

“A report must be published only if it has been approved in the past seven days.”

$\text{publish}(r) \rightarrow \blacklozenge_{[0,7d)} \text{approve}(r)$



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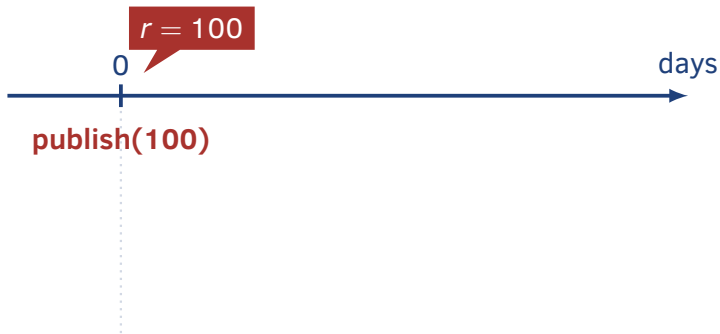
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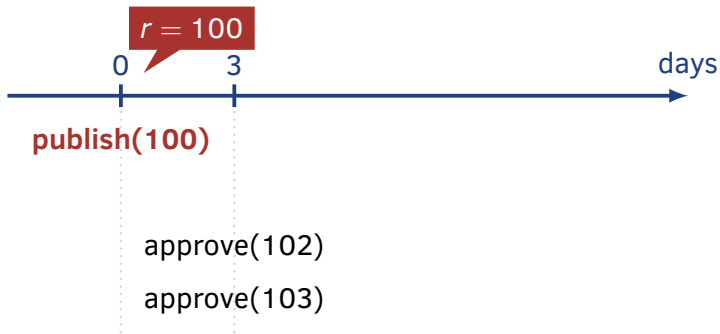
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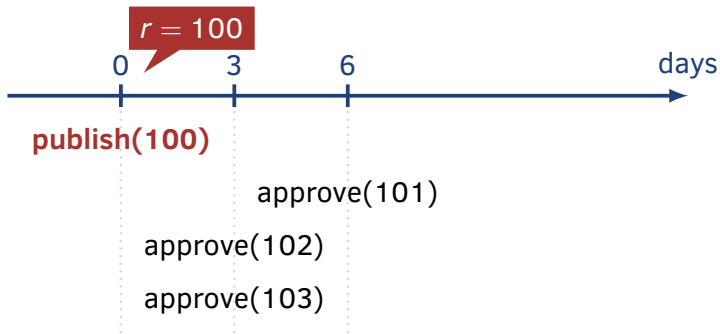
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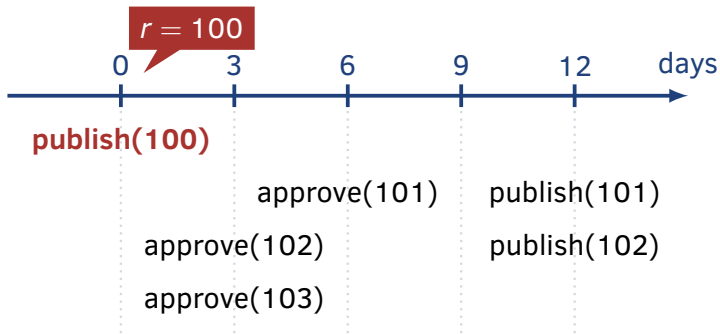
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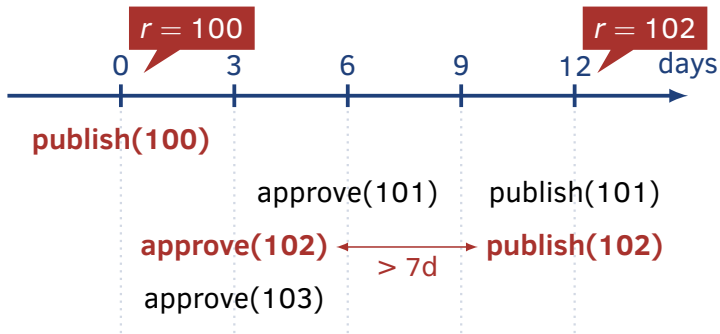
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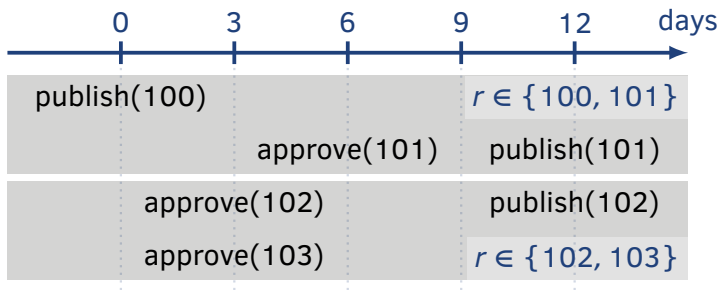
slicing variable



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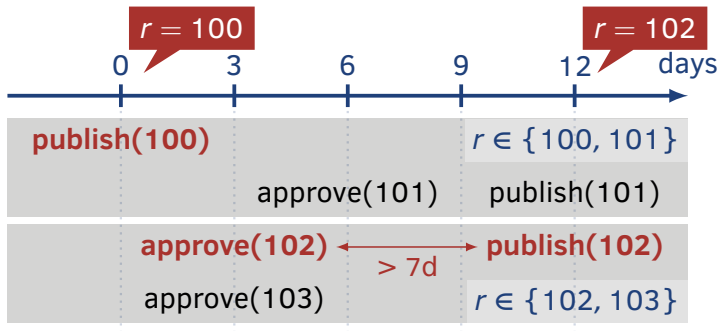




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# Problem 1: Too Much Data Duplication

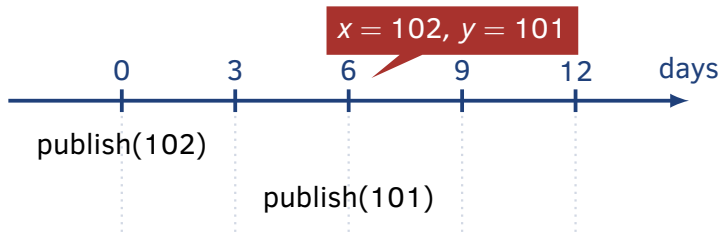
“IDs of published reports must increase over time.”

$$(\blacklozenge \text{publish}(x)) \wedge \text{publish}(y) \rightarrow x \leq y$$

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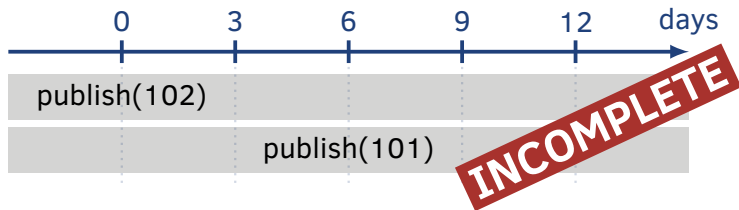
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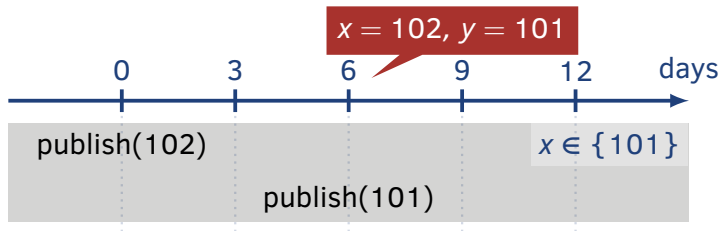
Completeness: all violations are detected

Soundness: all detected violations are true

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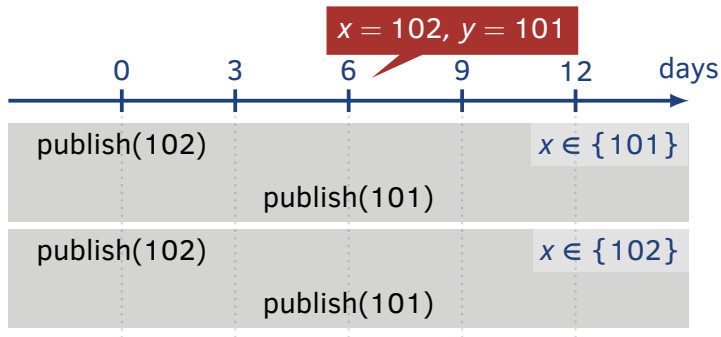
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## Problem 2: How to Slice?

Complex formulas:

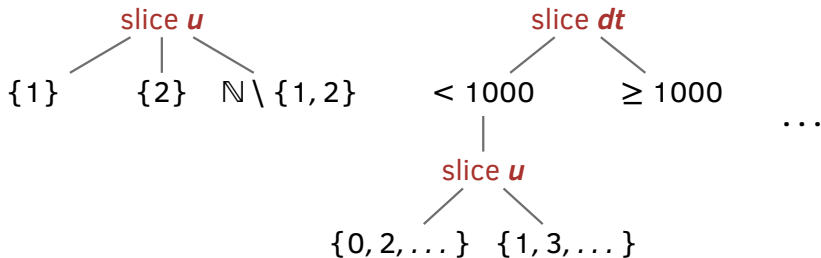
$$\begin{aligned} & \text{delete}(u, \text{db1}, dt) \wedge dt \not\approx \text{unknown} \rightarrow \\ & \left( \blacklozenge_{[0,1s)} \blacklozenge_{[0,30h)} \exists u'. \text{delete}(u', \text{db2}, dt) \right) \vee \\ & \left( \left( \blacklozenge_{[0,1s)} \blacklozenge_{[0,30h)} \exists u'. \text{insert}(u', \text{db1}, dt) \right) \wedge \right. \\ & \quad \left. \left( \blacksquare_{[0,30h)} \square_{[0,30h)} \neg \exists u'. \text{insert}(u', \text{db2}, dt) \right) \right) \end{aligned}$$

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Many possible choices:



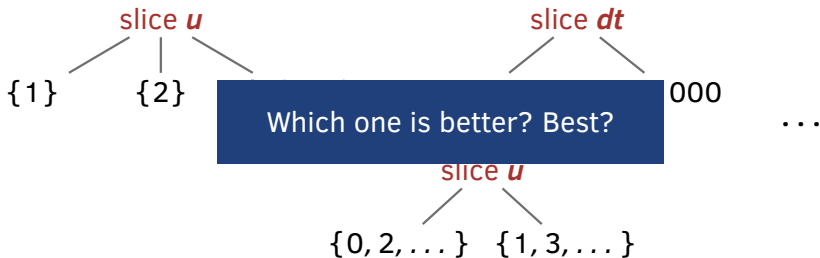


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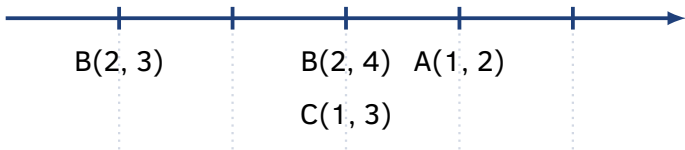
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# Our Solution

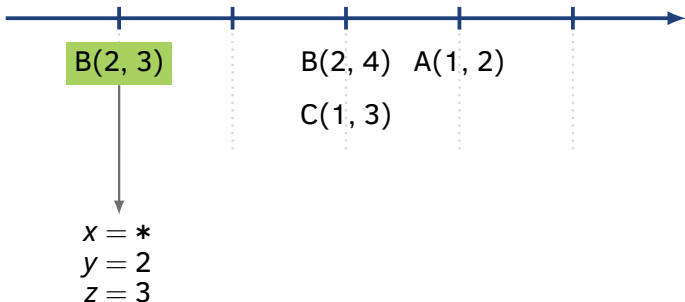
## Solution 1: Joint Data Slicer

$$A(x, y) \wedge (\blacklozenge B(y, z)) \rightarrow \blacklozenge C(x, z)$$



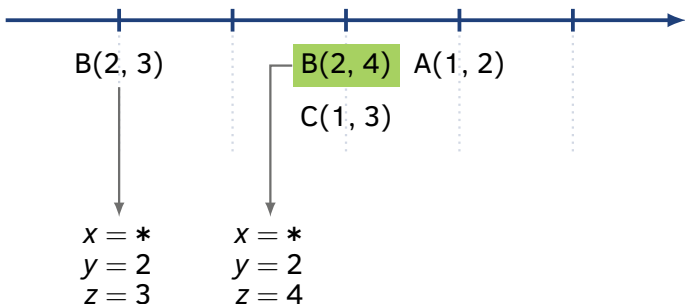
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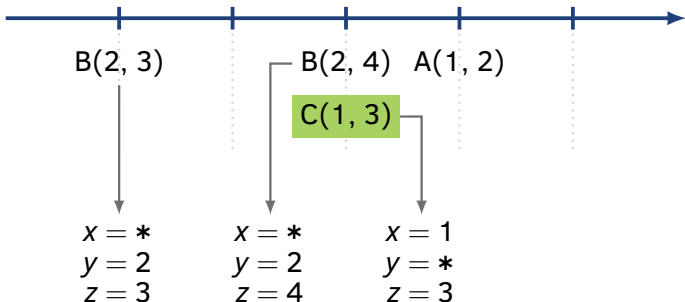
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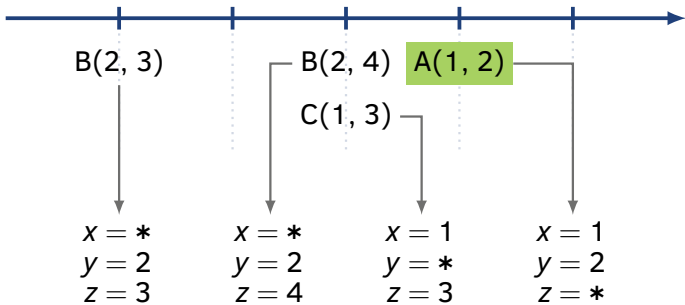
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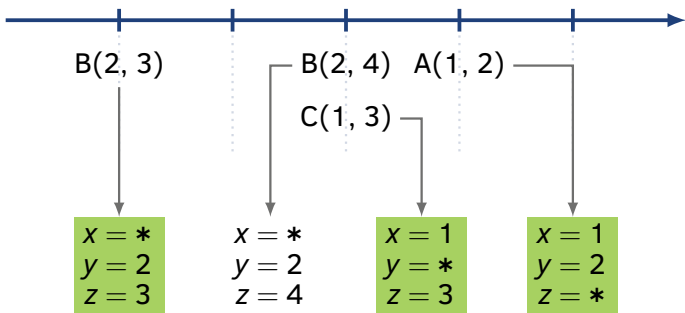
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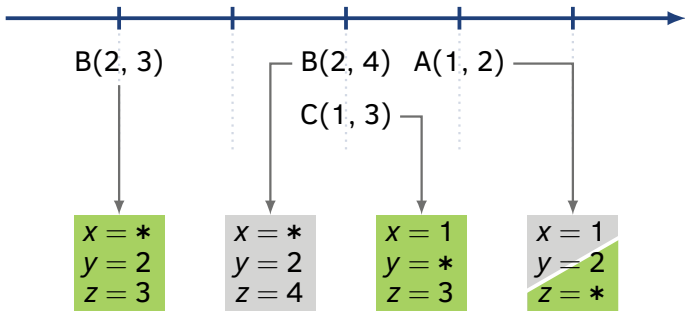
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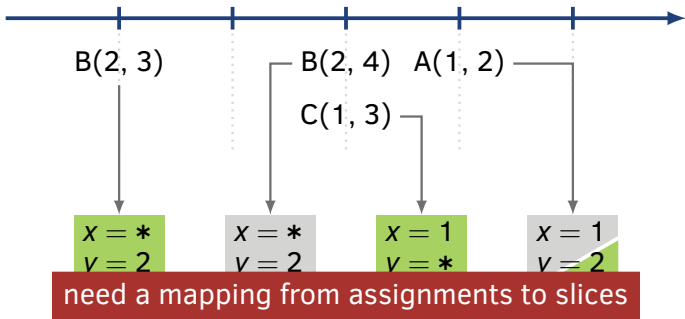
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$$A(x, y) \wedge B(y, z) \wedge C(x, z).$$

- This problem has been studied by the database community!
- Hypercube algorithm (Afrati and Ullman 2011, and others)
- Condition is only sufficient, not necessary

## Solution 2: Hypercube

$$A(x, y) \wedge (\blacklozenge B(y, z)) \rightarrow \blacklozenge C(x, z)$$

Free variables  $x, y, z$

$n$  monitors

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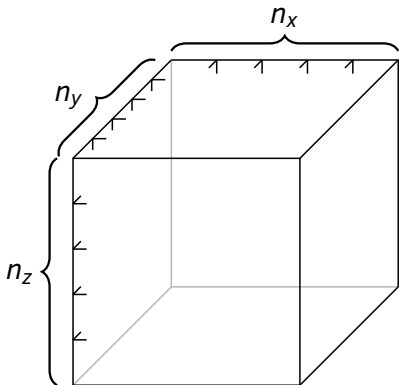
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Shares  $n_x, n_y, n_z$

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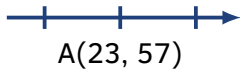


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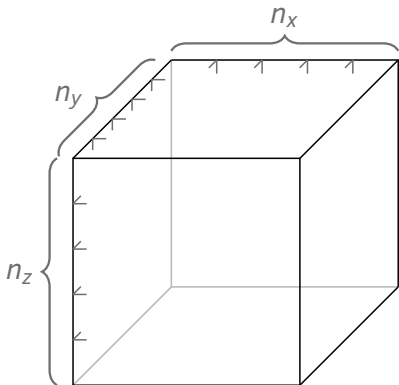
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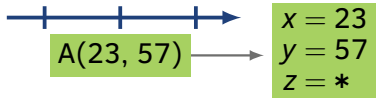


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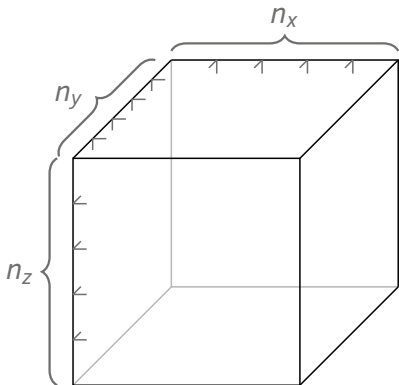
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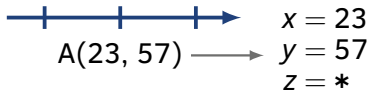


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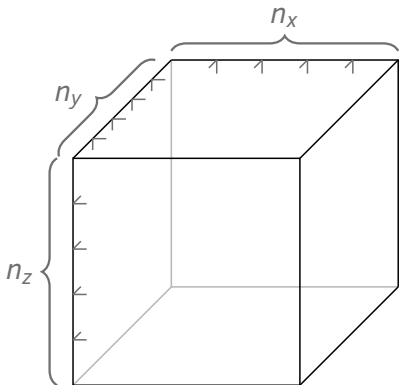
Hash functions

$$f_x : D \rightarrow \{1, \dots, n_x\}$$

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$$f_z : D \rightarrow \{1, \dots, n_z\}$$

$D$ : set of data values

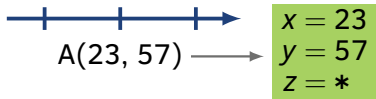


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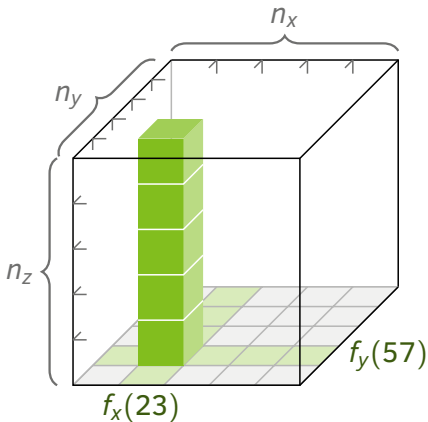
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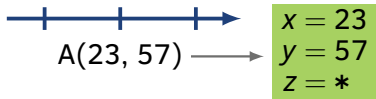


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optimized using event frequency statistics

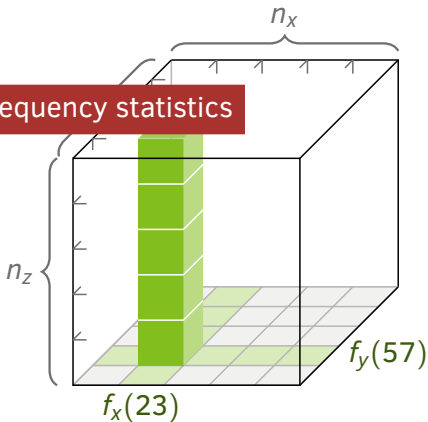
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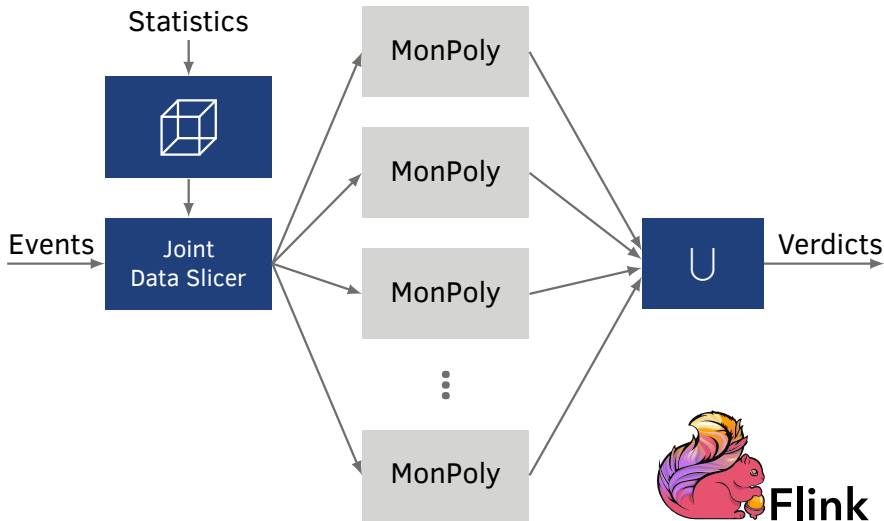
$$f_y : D \rightarrow \{1, \dots, n_y\}$$

$$f_z : D \rightarrow \{1, \dots, n_z\}$$

$D$ : set of data values



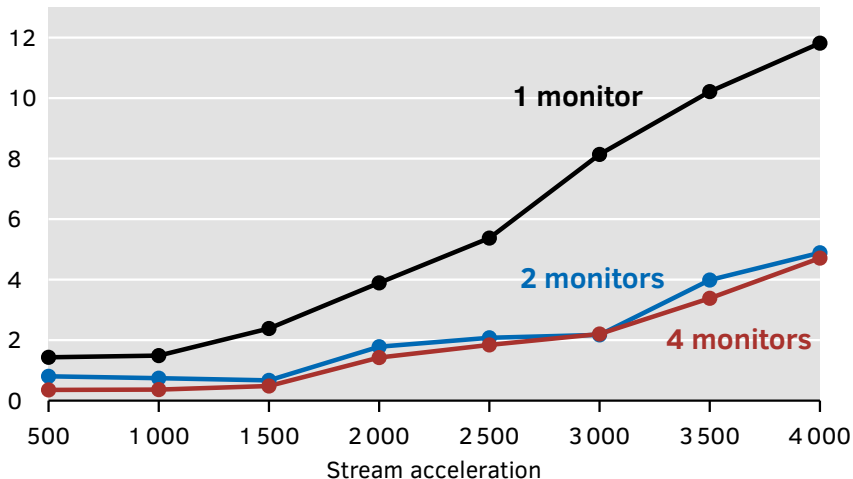
# Our Current Implementation



# Evaluation (1)

“Nokia” data excerpt, *insert* formula, with fault-tolerance

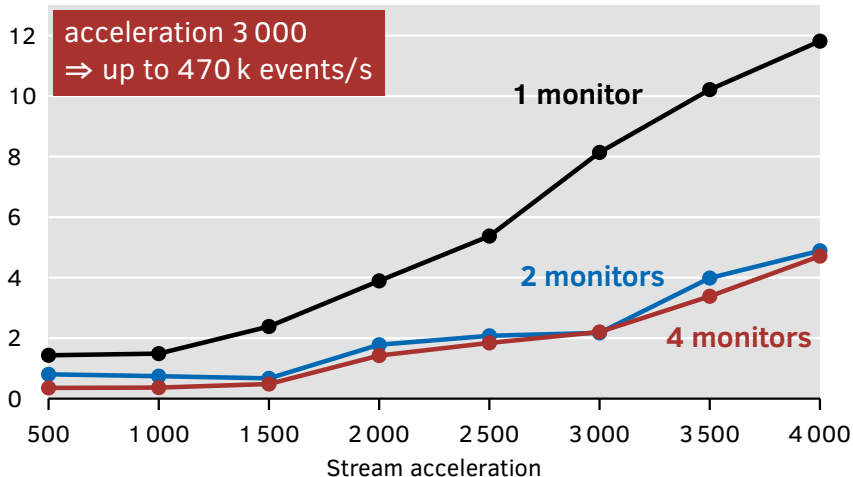
Max. latency [s] – lower is better



# Evaluation (1)

“Nokia” data excerpt, *insert* formula, with fault-tolerance

Max. latency [s] – lower is better

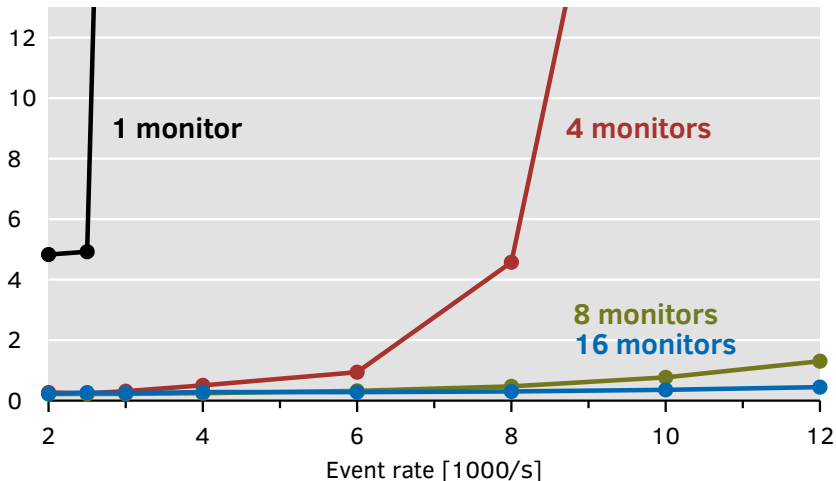




## Evaluation (2)

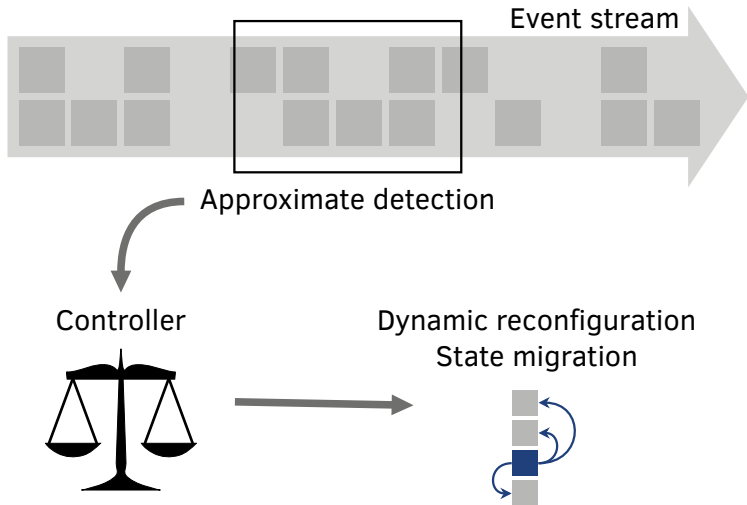
Random data, *triangle* formula, with fault-tolerance & statistics

Max. latency [s] – lower is better

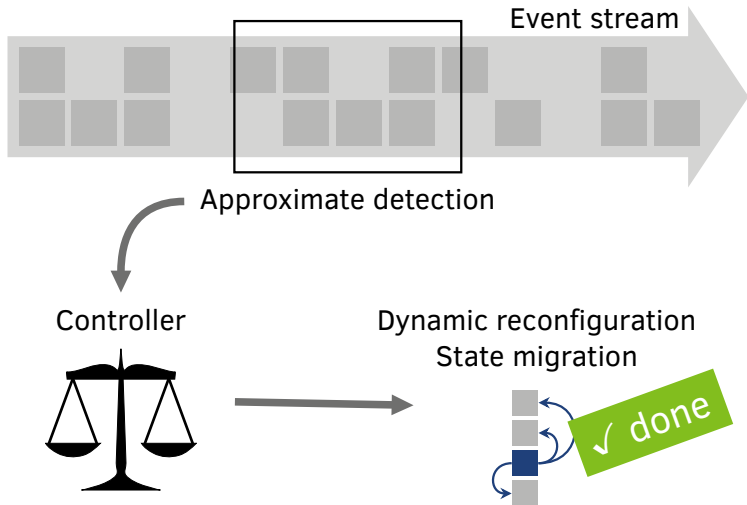


# Future Work & Conclusion

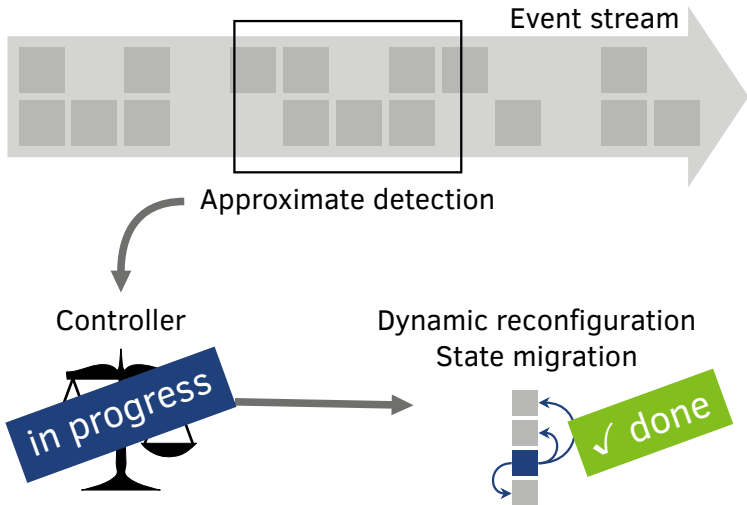
# Adapting to Changing Statistics



# Adapting to Changing Statistics

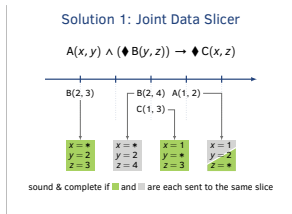


# Adapting to Changing Statistics



# Scalable Online First-Order Monitoring

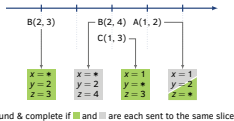
# Scalable Online First-Order Monitoring



# Scalable Online First-Order Monitoring

## Solution 1: Joint Data Slicer

$$A(x, y) \wedge (\diamond B(y, z)) \rightarrow \diamond C(x, z)$$



## Solution 2: Hypercube

$$A(x, y) \wedge (\diamond B(y, z)) \rightarrow \diamond C(x, z)$$

Free variables  $x, y, z$   
 $n$  monitors

Shares  $n_x, n_y, n_z$   
 $n = n_x \cdot n_y \cdot n_z$

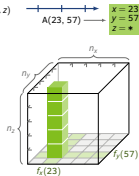
Hash functions

$$f_x: D \rightarrow \{1, \dots, n_x\}$$

$$f_y: D \rightarrow \{1, \dots, n_y\}$$

$$f_z: D \rightarrow \{1, \dots, n_z\}$$

$D$ : set of data values

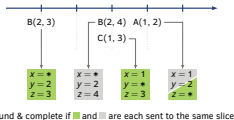




# Scalable Online First-Order Monitoring

## Solution 1: Joint Data Slicer

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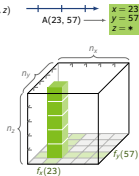
Hash functions

$$f_x: D \rightarrow \{1, \dots, n_x\}$$

$$f_y: D \rightarrow \{1, \dots, n_y\}$$

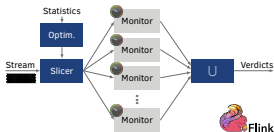
$$f_z: D \rightarrow \{1, \dots, n_z\}$$

$D$ : set of data values



## Slicing the Event Stream

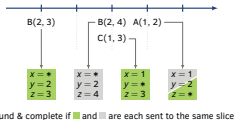
- Reuse existing monitoring algorithm (MonPoly)
- Split event stream into slices



# Scalable Online First-Order Monitoring

## Solution 1: Joint Data Slicer

$$A(x, y) \wedge (\diamond B(y, z)) \rightarrow \diamond C(x, z)$$



## Solution 2: Hypercube

$$A(x, y) \wedge (\diamond B(y, z)) \rightarrow \diamond C(x, z)$$

Free variables  $x, y, z$   
 $n$  monitors

$$A(23, 57) \rightarrow \begin{matrix} x = 23 \\ y = 57 \\ z = * \end{matrix}$$

Shares  $n_x, n_y, n_z$   
 $n = n_x \cdot n_y \cdot n_z$

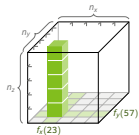
Hash functions

$$f_x: D \rightarrow \{1, \dots, n_x\}$$

$$f_y: D \rightarrow \{1, \dots, n_y\}$$

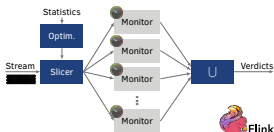
$$f_z: D \rightarrow \{1, \dots, n_z\}$$

$D$ : set of data values

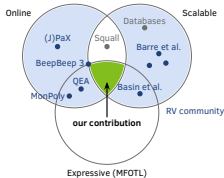


## Slicing the Event Stream

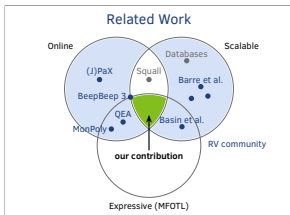
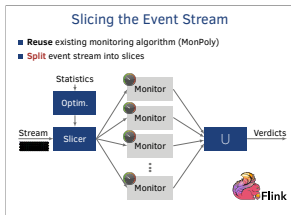
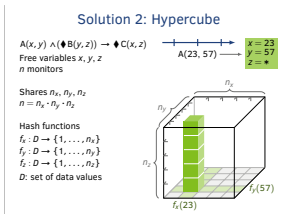
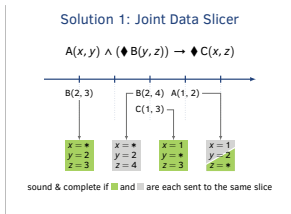
- Reuse existing monitoring algorithm (MonPoly)
- Split event stream into slices



## Related Work



# Scalable Online First-Order Monitoring



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